

# Welcome to Luke's Tailored Tutoring Inc. (Mathematics) 

We are delighted that you are joining the team! This guide will give you specific information to help you get started with us.

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## WHO ARE WE?

## Our Objective

Our goal is to help each student in their studies

## ELEMENTARY SCHOOL: PRIMARY

## GRADE 1

- Learn the basics of time and money
- Counting in intervals of ones, twos, fives, and tens
- Learning how to count to 100
- Adding and subtracting random numbers up to 20
- Place value up to 10


## GRADE 2

- Learn perimeter, area, and basic shapes
- Counting in intervals of fives, tens, and twenty-five
- Learning how to count backwards from 50
- Adding and subtracting random numbers between 10 and 100
- Place value up to 100


## GRADE 3

- Using grid paper to draw congruent shapes, quadrilaterals, and right angles
- Revise, polish, and produce their writing
- Counting in intervals of tens, twenties, twenty-fives, and hundreds
- Adding and subtracting random numbers between 100 and 999
- Division and multiplication of single-digit numbers
- Place value up to 1,000


## ELEMENTARY SCHOOL: JUNIOR

## GRADE 4

- Understanding the patterns, in addition, subtraction, and multiplication with steps missing
- Converting decimals from halves, fifths, and tenths
- Dividing and multiplying two-digit numbers
- Basics of fractions
- Adding and subtracting random numbers between 1000 and 10,000
- Division and multiplication of single-digit numbers
- Place value up to 100,000


## GRADE 5

- Understanding the patterns, in addition, subtraction, multiplication, and division with steps missing
- Using grid paper to draw angles such as acute, right, obtuse, and straight
- Rounding decimal amounts to the nearest hundredth
- Converting different units of measurement such as grams to kilograms, and centimetres to meters
- Arranging fractions with similar denominators
- Adding and subtracting random numbers between 10,000+
- Dividing and multiplying two-digit numbers
- Place value up to $1,000,000$


## GRADE 6

- Learning the basics of Probability
- Learning the lines of Symmetry
- BEDMAS introduction when learning Order of Operations
- Learning conversion between different systems such as pounds to kilograms, and yards to meters
- Rounding decimal amounts to the nearest thousandth
- Converting different units of measurement such as grams to kilograms, and centimetres to meters
- Adding and subtracting fractions with different denominators
- Dividing and multiplying four-digit numbers


## ELEMENTARY SCHOOL: INTERMEDIATE

## GRADE 7

- Probability and the basics of percentages
- Learning the lines of Symmetry
- BEDMAS using " $x$ " and " $y$ " variables when completing Order of Operations
- Using grid paper to draw perpendicular, intersecting, and parallel lines
- Introduction to squares and square root formulas
- Introduction to integers
- Adding and subtracting mixed fractions


## GRADE 8

- Introduction to bar graphs, scatter plots, and histograms
- Breakdown of word problems into algebraic formulas
- Introduction to rates such as $\mathrm{km} / \mathrm{hr}$ and calculating distance
- Probability and the basics of percentages
- Using formulas to calculate the area and volume of basic 3D shapes
- Calculating percentages
- Multiplying and dividing fractions and decimals
- Dividing and multiplying integers and fractions
- Introduction to exponents


## SECONDARY SCHOOL

## GRADE 9 SUMMARY

Academic will cover all of these units. Applied will cover some of these units.

- Operations with Integers and Rational Numbers
- Algebraic Expressions and Formulas
- Pythagorean Theorem
- Graphing Linear Relationships
- Exponent Laws


## GRADE 9 ACADEMIC

- Perimeter, area, surface area, and volume problem-solving with missing values
- Recognizing the elements of linear relationships
- Solving linear equations with $y=m x+b$
- Introduction to Polynomials
- Rearranging equations to solve for a variable
- Problem-solving with exponents
- Creating bar graphs, scatter plots, and pie charts in Microsoft Excel


## GRADE 9 APPLIED

- Perimeter, area, surface area, and volume problem-solving refresher
- Identifying linear relations' properties
- Reviewing rates such as $\mathrm{km} / \mathrm{hr}$ and calculating distance
- Review of breaking down word problems into algebraic formulas
- Review of fractions and decimals


## GRADE 10 DETAILED SUMMARY

Academic will cover all of these units. Applied will cover some of these units.

| Unit 1 - Linear Systems <br> - Linear Equations <br> - Graphing Linear Equations <br> - Intersecting Lines <br> - Substitution/Elimination | Unit 2 - Coordinates and Geometry <br> - Simplifying Radicals <br> - Distance on a Plane <br> - Equation of a Circle <br> - The midpoint of a line Segment <br> - Classifying shapes on a plane <br> - Geometric Properties | Unit 3 - Factoring <br> - Multiplying by Monomials and Polynomials <br> - Common Factoring <br> - Factoring Simple Trinomials <br> - Factoring Complex Trinomials <br> - Factoring Difference of Squares |
| :---: | :---: | :---: |
| Unit 4-Quadratic Models <br> - Quadratic Relations <br> - Properties of Quadratic Relations <br> - The role of Zeros in Quadratics <br> - Standard Form/ Factoring Quadratic Expressions <br> - Solving Quadratic Equations | Unit 5-Quadratic Relations <br> - Vertex Form of a Quadratic Relation <br> - Transformations of Quadratics <br> - Symmetry to relate Standard form and Vertex form <br> - Max and Min Values/ Completing the square <br> - Quadratic formula and nature of roots | Unit 6 - Similar and Congruent <br> Triangles <br> - Conditions for Congruent Triangles <br> - Investigating and comparing triangles <br> - Modelling with Similar Triangles <br> - Similar Triangle Models |
| Unit 7-Trigonometry I <br> - The connection between slope and angle <br> - Primary Trigonometric Ratios <br> - Solving Problems using right triangle models and trigonometry | Unit 8 - Trigonometry II <br> - Investigating the Sine Law <br> - Proving and Using the Sine Law <br> - Adjusting the Pythagorean Theorem: Cosine Law |  |

## GRADE 10 ACADEMIC

- Introduction to solving right triangles using trigonometry $\mathrm{SOH}, \mathrm{CAH}, \mathrm{TOA}$
- Perimeter, area, surface area, and volume problem-solving with missing values
- Examining the fundamental characteristics of quadratic relations
- Rearranging equations to solve for a variable
- Problem-solving angles in non-right-angled triangles
- Solving equations using quadratic relations, $y=a x^{2}+b x+c$
- Solving Polynomials
- Introduction to Factoring


## GRADE 10 APPLIED

- Interpreting quadratic relation graphs to solve problems
- Rearranging quadratic expressions and equations
- Graphing and writing linear equations
- Solving surface area and volume problems
- Introduction to trigonometry


## GRADE 11 UNIVERSITY FUNCTIONS (MCR3U) DETAILED SUMMARY

| Unit 1 - Equivalent Algebraic <br> Expressions <br> - Factoring <br> - Adding and Subtracting and Multiplying Polynomials <br> - Simplifying Rational Expressions <br> - Multiplying and Dividing Rational Expressions <br> - Adding and Subtracting Rational Expressions | Unit 2-Quadratic Equations <br> - Simplifying Radicals <br> - Determining Maximum or Minimum of Quadratic Functions by Completing the Square <br> - Solving Quadratic Equations <br> - The Nature of the Root of a Quadratic Equation <br> - Determining in a Quadratic Equation <br> - Solving Linear-Quadratic Systems | Unit 3 - Representing Functions <br> - Domain and Range of a Relation <br> - Function Notation <br> - Properties of $f(x)=\sqrt{x}$ and $f(x)=1 / x$ <br> - Inverse Functions <br> - Horizontal and Vertical Translations of Functions <br> - Reflections of Functions <br> - Stretches of Functions <br> - Combinations of Transformations |
| :---: | :---: | :---: |
| Unit 4 - Exponential Functions <br> - Exponent Laws <br> - Rational Exponents <br> - Compare Rates of Change of Exponential Functions with Linear and Quadratic Functions <br> - Graphs of Exponential Functions <br> - Transformations of Exponential Functions <br> - Solving Problems Involving Exponential Functions | Unit 5 - Sequence and Series <br> - Sequences (Continuous vs Discrete) <br> - Arithmetic Sequences <br> - Geometric Sequences <br> - Recursion Formulas <br> - Pascal's Triangle and Expanding Binomials <br> - Arithmetic Series <br> - Geometric Series | Unit 6 - Financial Applications <br> - Simple Interest <br> - Compound Interest <br> - Present Value <br> - Amount of an Ordinary Annuity <br> - Present Value of an Ordinary Annuity <br> - Present Value or Future Value |
| Unit 7 - Trigonometry I <br> - Reviewing the Trigonometry of Right Triangles <br> - CAST Rule <br> - Special Triangles <br> - The Sine and Cosine Law <br> - The Sine Law: Ambiguous Case | Unit 8 - Trigonometry II <br> - Modelling Periodic Behaviour <br> - Spaghetti Trigonometry <br> - Sketching the Graphs of $f(x)=\sin x$ and $f(x)=\cos x$ <br> - Stretches of Periodic Functions <br> - Translations and Reflections of Trigonometric Functions <br> - Combinations of Transformations <br> - Applications of Sinusoidal Functions | Unit 9 - Trigonometric Identities <br> - Trigonometric Identities <br> - Solving Trigonometric Equations |

## GRADE 11 FUNCTIONS AND APPLICATIONS (MCF3M) DETAILED SUMMARY

| Unit 1 - Intro to Quadratic <br> Functions <br> - Identity Functions <br> - Domain and Range <br> - Analyze Quadratic Functions <br> - Stretches of Functions <br> - Translations of Functions <br> - Sketch and Graphs Using Transformations | Unit 2 - Factor Quadratic <br> Expressions <br> - Exploring Forms <br> - Comparing Forms <br> - Factoring $\mathrm{ax}^{2}+\mathrm{bx}+\mathrm{c}$ <br> - Factoring <br> - Solving Equations by Factoring | Unit 3-Represent Quadratic <br> Functions <br> - Complete the Square <br> - Quadratic Formula <br> - The Real Roots of Quadratic Equations <br> - Multiple Forms of Quadratic Functions <br> - Model with Quadratic Equations |
| :---: | :---: | :---: |
| Unit 4-Trigonometry <br> - Find the Length <br> - Find the Angle <br> - Solve Problems Using 2 Right Angles <br> - Sine Law <br> - Cosine Law | Unit 5 - Sine Function <br> - Periodic Motion and Behaviour <br> - Sine Function <br> - Transformations | Unit 6 - Exponential Functions <br> - The Exponent Rules <br> - Evaluate Powers with Integer Exponents <br> - Rational Exponents <br> - Model Data with Exponential Functions <br> - Exponential Functions and Their Properties <br> - Compare Linear, Quadratic, and Exponential Function <br> - Growth and Decay |
| Unit 7 - Finance I <br> - Explore Simple and Compound Interest <br> - The Compound Interest Formula <br> - Time Value of Money Calculator (TMV) Solver | Unit 8 - Finance II <br> - Future Value of an Ordinary Simple Annuity <br> - Present Value of an Ordinary Simple Annuity <br> - The Effects of Changing The Conditions of an Ordinary Simple Annuity |  |

## GRADE 11 FOUNDATIONS FOR COLLEGE (MBF3C)

- Workplace-Readiness Training
- Management of Data
- Trigonometry and Geometry
- Financial Services
- Models in Mathematics


## GRADE 12 DATA MANAGEMENT (MDM4U)

## Unit 1 - Organization and analysis of data: Two Variable Stats

- Introducing the Importance of Data
- Recognizing Bias Data Collection Principles and Methods
- Analyzing Two-Variable Data
- Analyzing the Residuals and Outliers in Two Variable Data
- Interpreting Data
Unit 4 - Probability and probability distributions
- Introducing Experimental vs Theoretical Probability
- Learning About Mutually Exclusive and Non-Mutually Exclusive Events
- Understanding Independent and Dependent Events
- Exploring Probability Distributions and Expected Value
- Calculating Binomial Distribution and Hypergeometric Distribution
- Applying Normal Approximation to the Binomial Distribution

Unit 2- Data analysis: One variable stats, and the normal distribution

- Introducing One Variable Statistics
- Calculating Measures of Central Tendency
- Calculating Measures of Spread
- Learning About Normal Distribution and Z-Scores
- Applying Z-Scores to Discrete Data
- Exploring Confidence Intervals


## Unit 3-Permutations and combinations

- Introducing Organized Counting and the Fundamental Multiplicative Counting Principle
- Learning about Permutations

Factorials: Rule of Sum and Applications

- Understanding Combinations
- Counting Problems with Repeated Elements and Overlap
- Investigating Pascal Triangle and Problems using Combinations

GRADE 12 UNIVERSITY ADVANCED FUNCTIONS (MHF4U)

## Unit 1-Algebraic Operations

- Operations With Polynomials
- Common Factors \& Trinomials
- Special Factoring Methods
- Dividing A Polynomial By A Polynomial
- The Remainder Theorem
- The Factor Theorem
- Factoring Sums \& Differences of Cubes


## Unit 4-Transformations Of Trigonometric

## Functions

- Introduction to Periodic Functions
- Graphing Primary/Reciprocal Trig Functions
- Varying The Vertical Displacement of $\sin \theta$ $\& \cos \theta$
- Varying The Phase Shift of $\sin \theta \& \cos \theta$
- Varying The Amplitude of $\sin \theta \& \cos \theta$
- Varying The Period of $\sin \theta \& \cos \theta$
- Connecting Functions \& Their Graphs
- Rescaling The Horizontal Axis
- Applying General Sinusoidal Functions


## Unit 7 - Logarithmic Functions

- Common Logarithms
- Laws of Logarithms - Mult. \& Division
- Laws of Logarithms - Powers \& Roots
- Introduction to Logarithmic Functions
- Graphing Logarithmic Functions
- Logarithms As Exponents
- Laws of Logarithms - Bases Other Than 10


## Unit 2 - Polynomial Functions

- Polynomial Functions Terminology \& Facts
- The Shapes of Polynomial Functions
- End Behaviours of Polynomial Functions
- Solving Polynomial Equations
- Solving Polynomial Inequalities

Unit 3-Trigonometric Ratios \& Equations

- Measuring Angles With Radians
- Coterminal Angles \& Reciprocal Trig Ratios
- Trigonometric Ratios of Special Angles
- Trigonometric Ratios of Obtuse Angles
- Trig Ratios of Angles In Standard Position
- Exploring the Unit Circle

Unit 6-Exponential Functions

- Simplifying Exponential Expressions
- Graphing Exponential Functions
- Applications of Exponential Functions
- Using Exponential Functions to Make Comparisons

GRADE 12 CALCULUS AND VECTORS (MCV4U)

| Unit 1 - Vectors - Introduction to <br> Vectors <br> - Introduction to Vectors <br> - Vector Addition \& Subtraction <br> - Vector Operations <br> - Applications of Vectors Velocity <br> - Applications of Vectors - Force | Unit 2 - Vectors - Algebraic Vectors <br> - Algebraic Vectors (2D) <br> - Algebraic Vectors (3D) <br> - Dot Product <br> - Applications of Dot Product Work <br> - Cross Product <br> - Applications of Cross Product Area \& Torque | Unit 3 - Vectors - Lines and Planes <br> - Matrices <br> - Equation of a Line (2D) <br> - The Intersection of Lines (2D) <br> - Equation of a Line (3D) <br> - The Intersection of Lines (3D) <br> - Vector Equation of a Plane <br> - Scalar Equation of a Plane <br> - The Intersection of Lines \& Planes <br> - The Intersection of Planes (Geometric Representation) <br> - Intersection of Planes |
| :---: | :---: | :---: |
| Unit 4-Calculus - Introduction to <br> Calculus \& Derivatives <br> - Polynomial Review <br> - Rate of Change <br> - The Derivative Function <br> - Power Rule <br> - Chain Rule <br> - Product Rule <br> - Derivative Practice <br> - Derivatives of Rational Expressions <br> - Derivative Problem Solving | Unit 5-Calculus - Curve Sketching <br> - Sketching Intercepts \& Asymptotes <br> - Critical Points <br> - Increasing/ Decreasing <br> - Points of Inflection \& Concavity | Unit 6-Calculus - Applications of Derivatives <br> - Velocity \& Acceleration <br> - Maximum \& Minimum <br> - Max/Min Displacement, Velocity \& Acceleration <br> - Optimization - Measurement <br> - Optimization - Finance |
| Unit 7-Calculus - Derivatives of Trigonometric Functions <br> - Trigonometry Review <br> - Derivative of $y=\operatorname{Sin} X$ and $y=$ CosX <br> - Chain Rule <br> - Product Rule <br> - Derivative Practice Max/Min <br> - Optimization | Unit 8 - Calculus - Derivatives of Exponential Functions <br> - Exponent \& Log Review <br> - Derivatives of Exponential Functions <br> - Chain Rule <br> - Product Rule <br> - Derivative Practice <br> - Maximum \& Minimum <br> - Optimization Problems |  |

